

## SECTION A

### Attempt all questions

1. Express 18 and 42 each as a product of its prime factors and hence find their highest common factor (HCF).
2. Express  $2.10303\dots$  in the form  $2\frac{a}{b}$ , where a and b are integers.
3. Given that  $f(x)=2\sqrt{x}+6$ , find the value of x for which  $f(x)=16$
4. Find the equation of a line passing through point (0, -5) and is perpendicular to the line  $y + 3x = 1$
5. Simplify the following as far as possible,

$$\log_2 4 - \frac{1}{2} \log_3 8 + \log_2 8$$

6. Given that position vector  $\mathbf{OP} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$  and  $\mathbf{OQ} = \begin{pmatrix} 4 \\ -1 \end{pmatrix}$  Find the coordinates of the mid-point of vector  $\mathbf{PQ}$
7. Two similar conical flasks have heights of 32.4cm and 97.2cm. If the volume of the small flask is  $3016\text{cm}^3$ , find the volume of the big flask.
8. A tourist has US\$ 1200 which he changes to Uganda shillings (Ug. Shs) at a rate of \$1 = Ug. Shs 3500. If he has a balance of Ug. Shs 900,000 after all expenses find;
  - (a) the amount of money spent in Ug. Shs.
  - (b) his balance in US dollars
9. The number of people who play football (F) or basketball (B) is twice the number of people who play F and B. If  $n(F) = 9$  and  $n(B) = 6$ , how many play both games?
10. The quantity V varies directly as H and inversely as the square of W. Given that when  $W = 50$ ,  $H = 100$  and  $V = 80$ , find W, when  $H = 320$  and  $V = 100$ .

## SECTION B (60 MARKS)

*Attempt any five questions in this section. All questions carry equal marks.*

11. A quantity R varies partly as the cube of V. When  $V = 20$ ,  $R = 416$  and when  $V = 40$ ,  $R = 3264$ .
  - (a) Form an equation relating R and V
  - (b) Determine the value of R when  $V = 30$

12. The functions  $f$  and  $g$  are defined by  $f(x) = \frac{x}{x-5}$  and  $g(x) = x+4$ . Find;

- (a)  $g^{-1}(10)$
- (b)  $f^{-1}(x)$  and hence  $f^{-1}(6)$
- (c) the value of  $x$  for which  $gf(x) + fg(x) = 0$

13. In a mathematics class the teacher told students to bring a pen (P), a graph book (G) and a ruler (R) for use. During the next lesson it was found out that only 16 students brought all the items. 5 students did not have any of the items. 13 did not have a pen, 14 did not have a graph book and 20 did not have a ruler. One student only had a pen, 2 students had only a graph book and no student had only a ruler.

- (a) Represent the above information on a Venn diagram
- (b) How many students
  - (i) were in the class?
  - (ii) had a pen and a ruler only?

c) If a student is selected at random find the probability that he had;

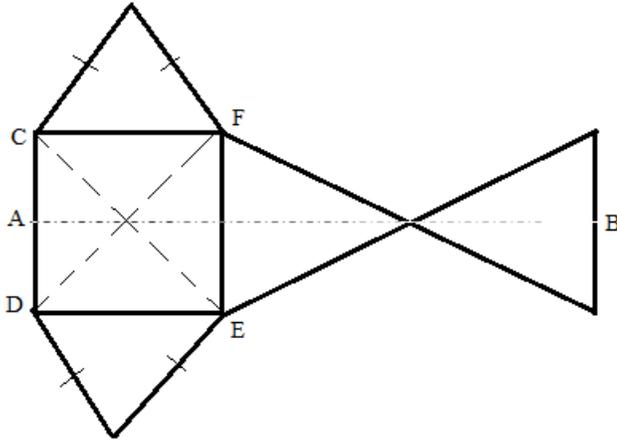
- (i) at least 2 items.
- (ii) only one item

14. A lorry set off from Tororo at 0730 hours at a steady speed of 40km/hr to Kampala, a distance of 180km away. After travelling for 2 hrs it stopped and rested for 1 and  $\frac{1}{2}$  hrs, then continued at a steady speed of 50km/hr for the rest of the journey. A car also set off from Kampala to Tororo at the same time as the lorry at a steady speed of 60km/hr but suddenly reduced its speed after 2hrs to 15km/hr due to some mechanical fault for the remaining journey.

Using scales of 1cm to 10km and 1cm to 30 minutes on the vertical and horizontal axes respectively:

- (a) Draw distance time graphs showing the routes of the two vehicles.
- (b) Using your graphs determine the
  - (i) distance between the two vehicles after two hours.
  - (ii) difference in time of arrival at respective towns.

15. The diagram below shows a square CDEF with diagonals CE and DF each =  $\sqrt{200}$  cm and four congruent isosceles triangles representing the net of a pyramid on a square base.



Given that  $AB = 46\text{cm}$ ;

- (a) Draw a sketch of the pyramid.
- (b) Calculate the;
  - (i) height of the vertex of the pyramid above the base
  - (ii) angle between two opposite slanting planes
  - (iii) volume of the pyramid

16. (a) Calculate the simple interest on Shs. 990,000 for 8 months at a rate of  $5\frac{1}{2}$  per annum.

(b) The income tax rates of a certain country are shown in the table below:

Taxable income(shs)	Rate (%)
01 - 200,000	6
200,001-500,000	13
500,001-900-000	20
900-000 and above	30

- (i) Calculate the income tax an employee pays if the employees' taxable income is Ug.Shs 1,170.000.
- (ii) Given that the employees untaxed allowances is Shs 140,750/=. Find the employees net income.

15. In a triangle  $OPQ$  point  $R$  lies on the line  $PQ$  such that  $3PR = PQ$ . Point  $S$  lies on a line  $OQ$  and  $OS = \frac{1}{4}OQ$ , while  $T$  lies on line  $OR$  such that  $OT = TR$ . If  $OQ = \mathbf{q}$  and  $OP = \mathbf{p}$  express in terms of  $\mathbf{p}$  and  $\mathbf{q}$  the vectors.

(a) (i)  $PQ$     (ii)  $OR$     (iii)  $PT$

(b) Show that  $PT : TS = 2:1$